



THE UNIVERSITY *of* EDINBURGH  
**informatics**

Applied Machine Learning (AML)

**Class Starting at 4:10pm**

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# Applied Machine Learning

Week 4: Linear Regression and Decision Trees

*This session will be recorded.*

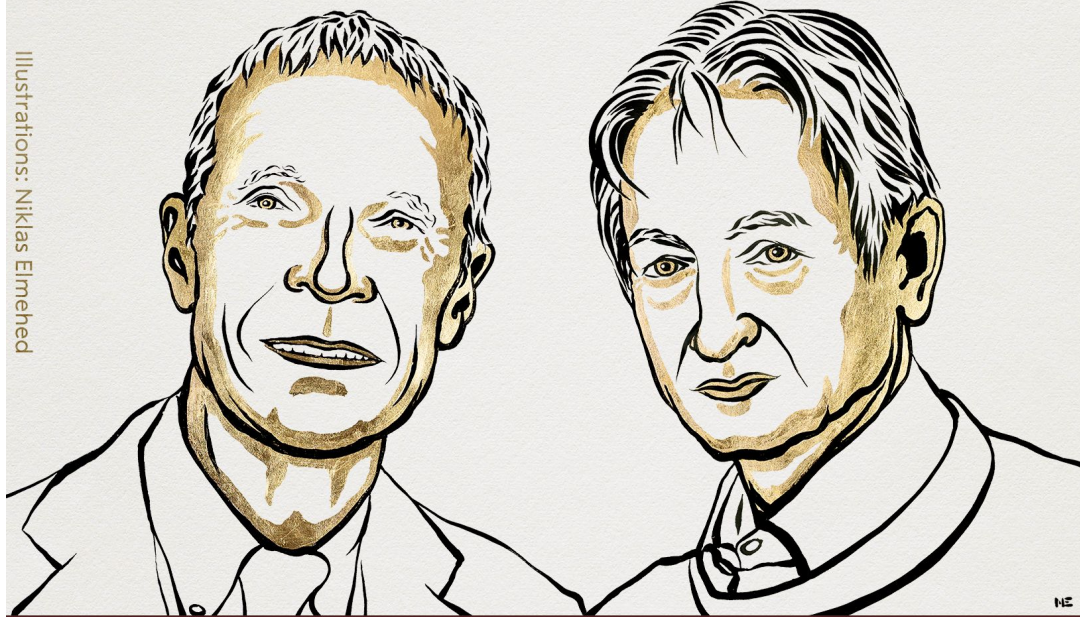
# Overview

- 1) Discussion of Week 3's topics
- 2) Quiz questions
- 3) Outline your tasks this for week

<https://tinyurl.com/aml2024>

# THE NOBEL PRIZE IN PHYSICS 2024

Illustrations: Niklas Elmehed



John J. Hopfield

Geoffrey E. Hinton

“for foundational discoveries and inventions  
that enable machine learning  
with artificial neural networks”

THE ROYAL SWEDISH ACADEMY OF SCIENCES

# Lab and Tutorial Times

## Tutorials

Tutorial 8 (Fri 1pm, weeks 4, 6, 8, 10) has been removed from the timetable. If you were in that group you will have been assigned to a different group.

## Labs

Lab 8 (Fri 11am, weeks 3, 5, 7, 9) has been **incorrectly** removed from the timetable. If you were in that group, you will have been re-assigned to a different group. This may get changed back later this week.

Apologies for any inconvenience caused.

# Changing Lab/Tutorial Group

If your assigned time slot clashes with your other classes, you can submit a Group Change Request Form.

<https://www.ed.ac.uk/timetabling-examinations/timetabling/personalised-timetables/student-timetables>

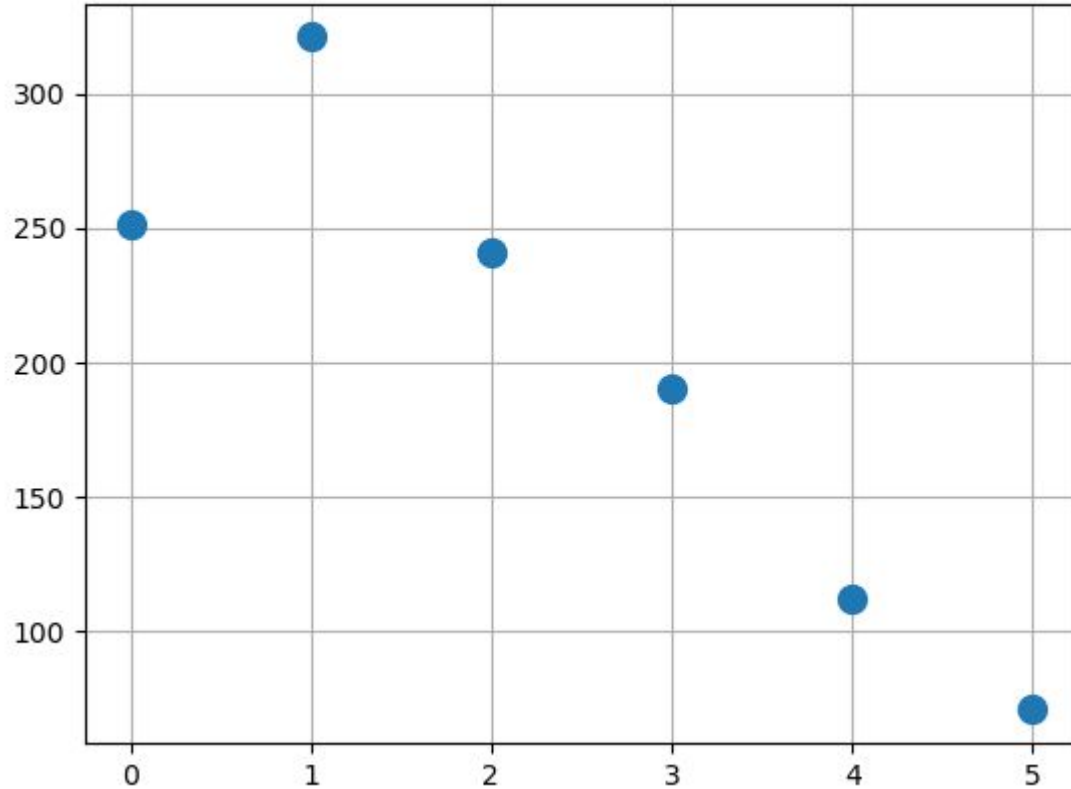
However, we encourage you to only do this if you have a conflict. Otherwise, you should stay with the group you have been assigned.

No need to contact the course organisers about this.

# Coursework

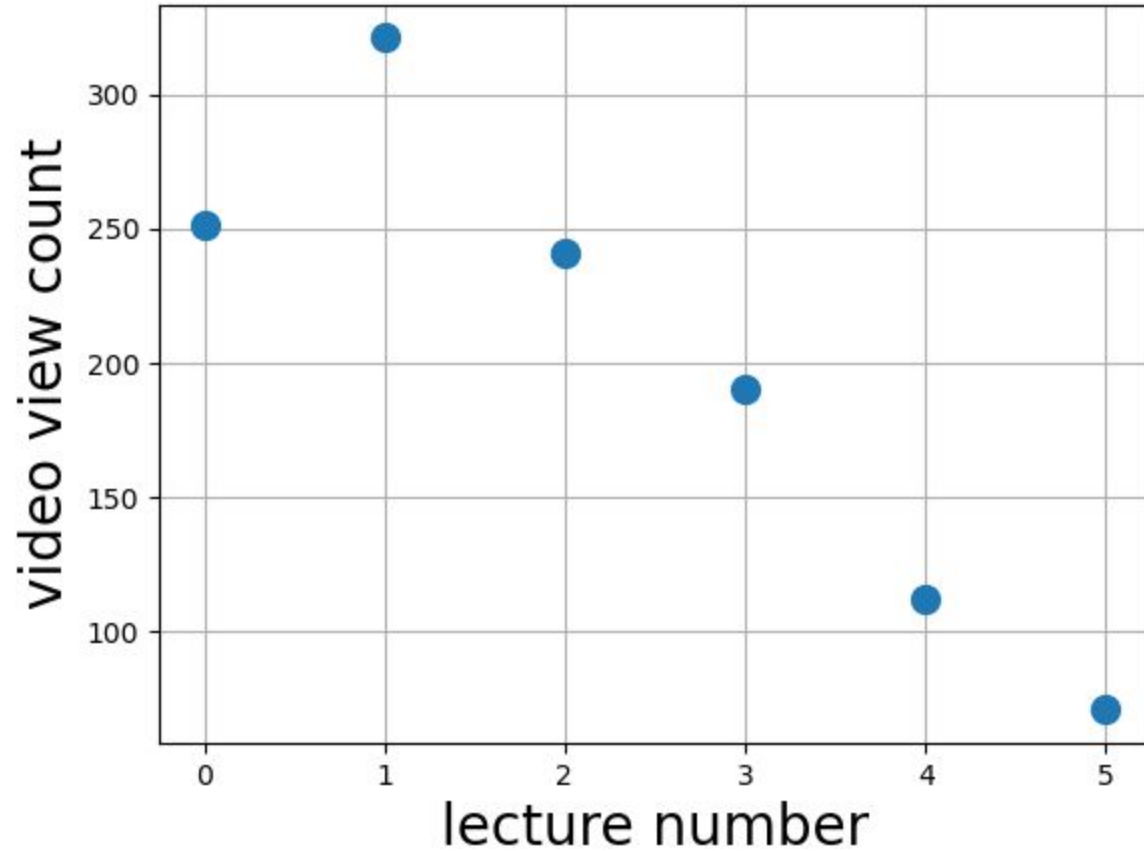
- Info available on course webpage
  - <https://groups.inf.ed.ac.uk/teaching/aml/mini-project>
- If you have not already been assigned a group, we will allocate you this week. This will be online ~tomorrow.
- If you have questions about the CW, check the FAQ, and if not answered, post them as private messages on Piazza.

# What data is this?

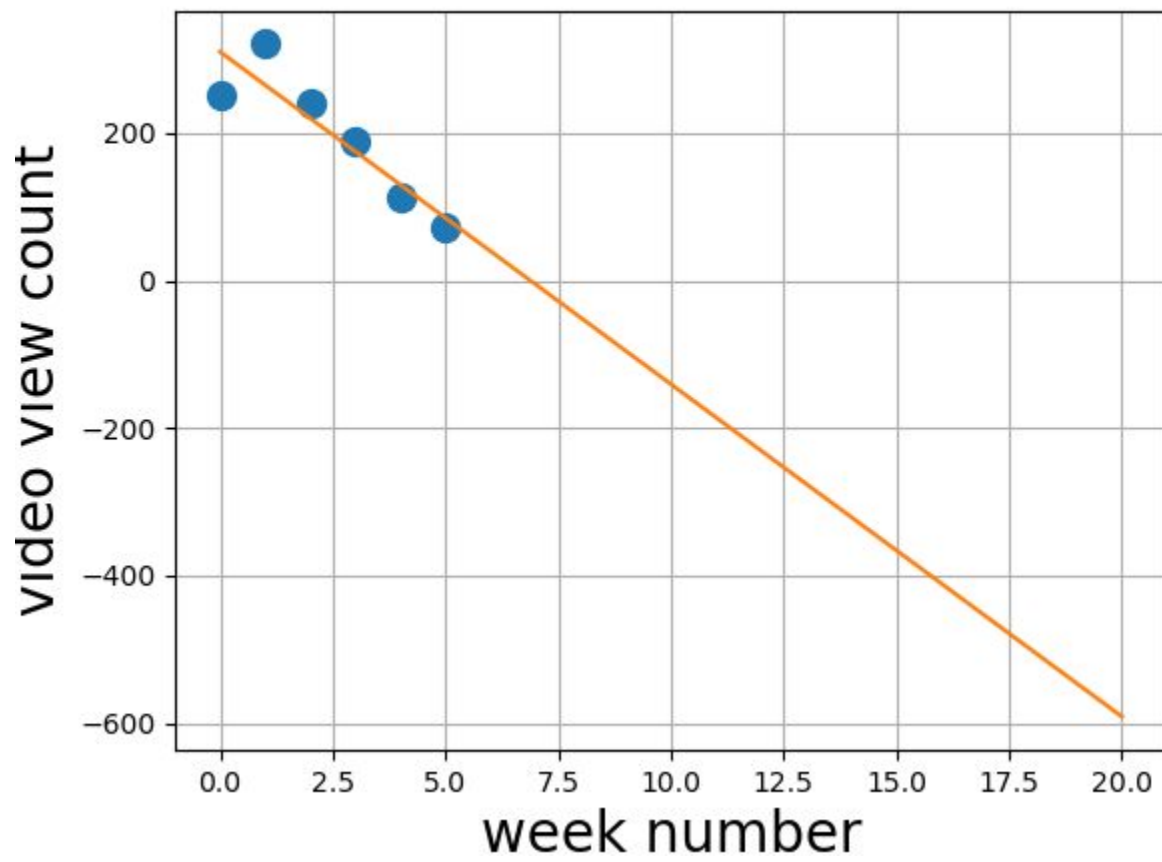




What data is this?



# Future trend?



# Interactive - Linear Regression

<https://mlu-explain.github.io/linear-regression>

# Quiz Questions

# Interactive - Decision Trees

<https://mlu-explain.github.io/decision-tree>

# Quiz Questions

# Polynomial Regression

- Up until now we have set  $\phi(x) = [1, x]^\top$
- However, we can transform our inputs in different ways
- One example is **polynomial regression**,  $\phi(x) = [1, x, x^2, \dots, x^M]^\top$
- Here, the dimensionality of our weights  $w$  will be the same as  $\phi(x)$

# Basis Functions

- We can easily transform the original features  $\mathbf{x}$  **non-linearly** into  $\phi(\mathbf{x})$  and perform linear regression on the transformed features

- For example, we can use a set of  $M$  basis functions

$$\phi(\mathbf{x}) = [1, \psi_1(\mathbf{x}), \psi_2(\mathbf{x}), \dots, \psi_M(\mathbf{x})]^\top$$

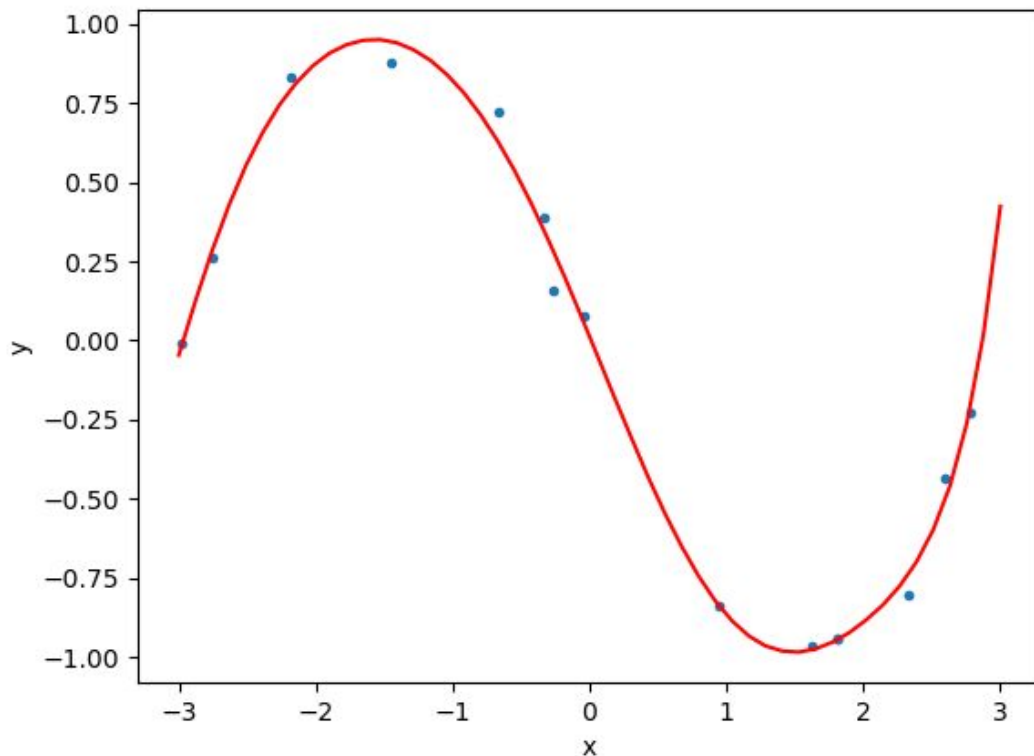
- Each of these basis functions takes a vector as input and outputs a scalar value



# Basis Functions

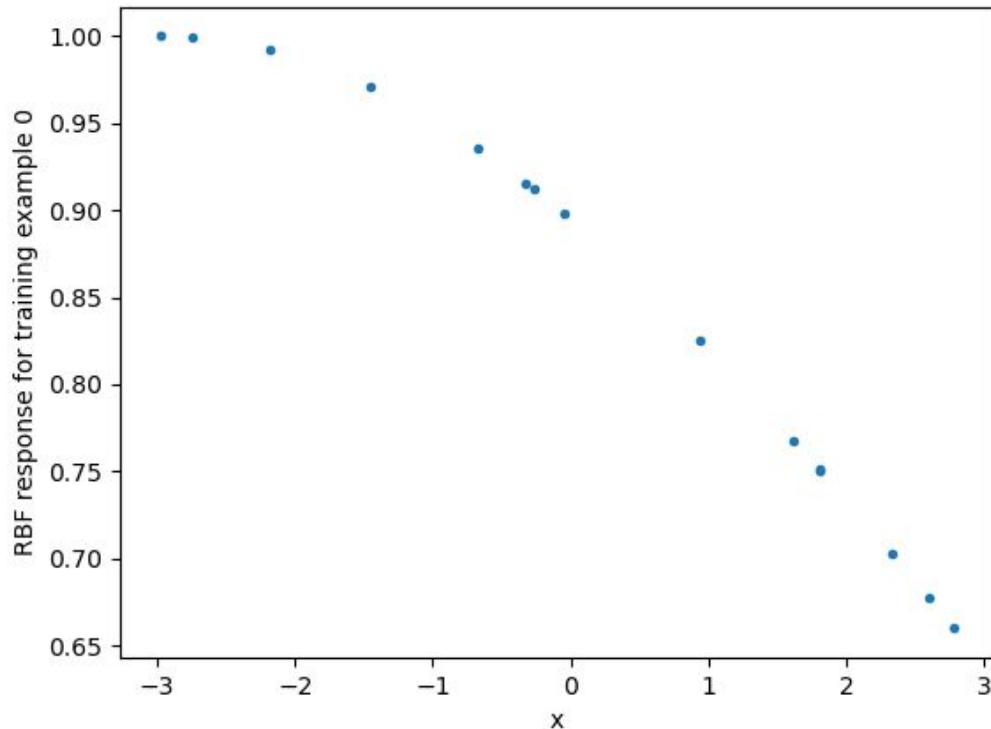
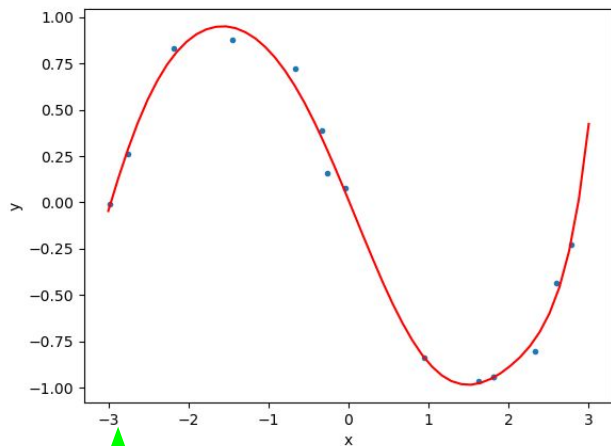
In this example, we have a RBF centred on each training point and we use the same value of  $\sigma^2$  for each

$$\phi(\mathbf{x}) = [1, \psi_1(\mathbf{x}), \psi_2(\mathbf{x}), \dots, \psi_M(\mathbf{x})]^\top$$



# Basis Functions

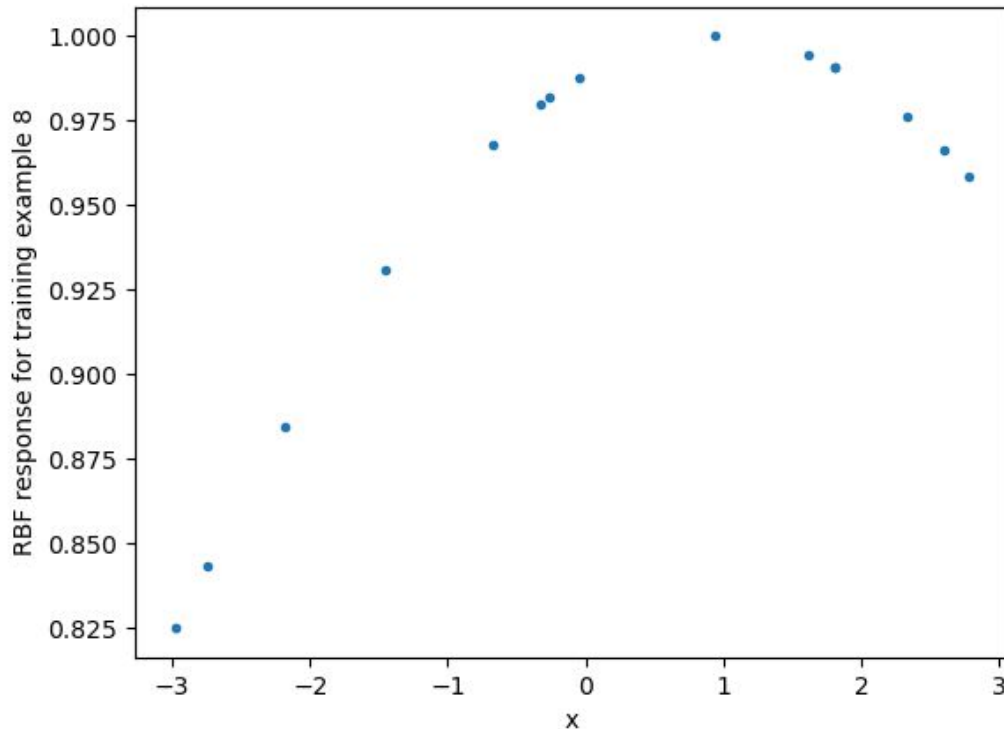
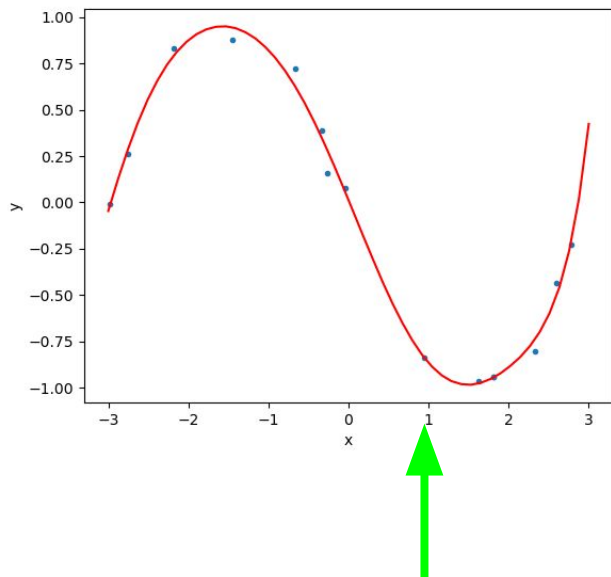
$$\psi_m(\mathbf{x}) = \exp\left(-0.5 \frac{\|\mathbf{x} - \mathbf{c}_m\|^2}{\sigma_m^2}\right)$$



Here we plot responses of the different RBFs for the first training example

# Basis Functions

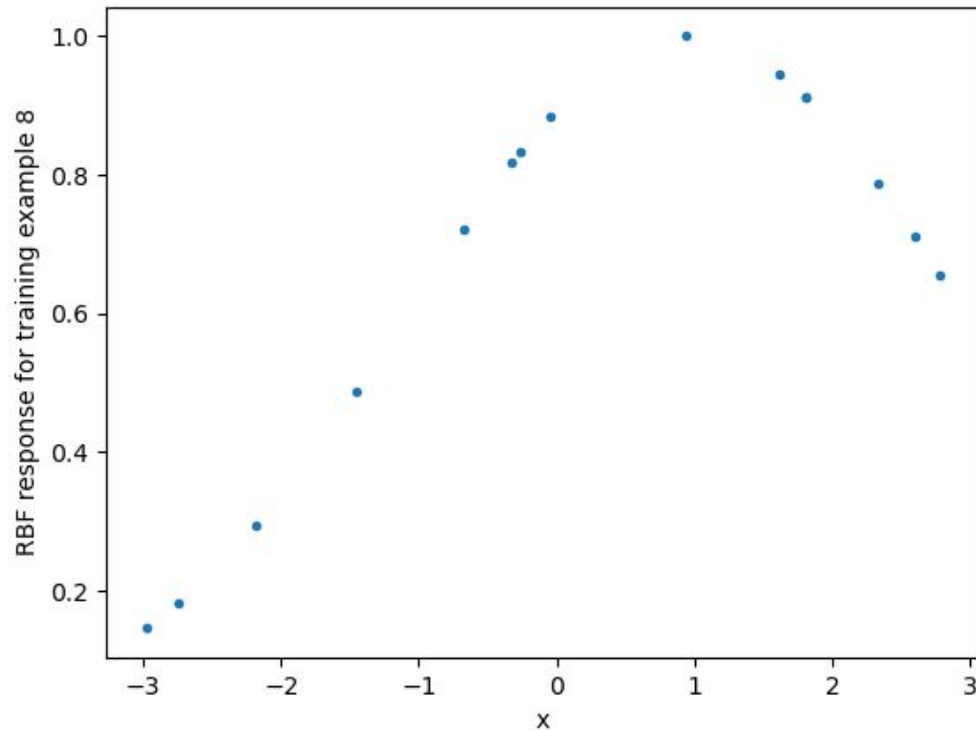
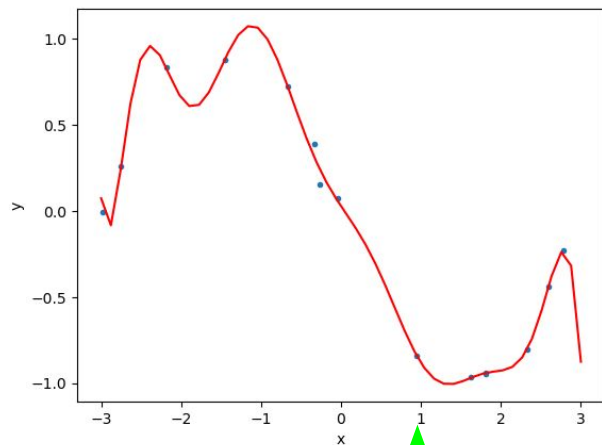
$$\psi_m(\mathbf{x}) = \exp\left(-0.5\frac{\|\mathbf{x} - \mathbf{c}_m\|^2}{\sigma_m^2}\right)$$



Here we plot responses of the different RBFs for a different training example

# Basis Functions

$$\psi_m(\mathbf{x}) = \exp\left(-0.5 \frac{\|\mathbf{x} - \mathbf{c}_m\|^2}{\sigma_m^2}\right)$$



Here we decrease the variance of the RBF

# Week 4: Your tasks for this week

- 1) Complete Tutorial 1 - solutions will be online next week
- 2) Watch the videos for Week 4 - **Representing Data** and **Exploratory Data Analysis**
  - a) Ask questions on Piazza if stuck
- 3) Start the coursework - due in Week 10
  - a) Groups will be online soon
  - b) We will discuss progress reports soon
- 4) Start Lab 2 - link in Week 5