

# It Takes a Village: Reasoning About Concurrent Processes

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Imperial College  
London

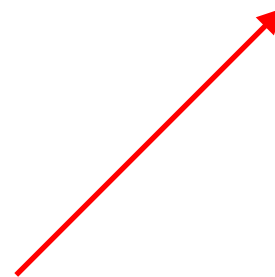
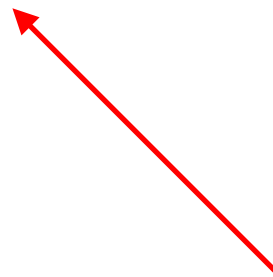
# Motivating Meta-Theory

Certified tool + reasoning environment

Reasoning

Certified code  
extraction

Mechanised  
Meta-theory



# Binary Session Types

- Do a case study:
  - Language Primitives and Type Discipline for Structured Communication-Based Programming Revisited, by Yoshida and Vasconcelos, 2007.



Available online at [www.sciencedirect.com](http://www.sciencedirect.com)



Electronic Notes in  
Theoretical Computer  
Science

Electronic Notes in Theoretical Computer Science 171 (2007) 73–93

[www.elsevier.com/locate/entcs](http://www.elsevier.com/locate/entcs)

Language Primitives and Type Discipline for  
Structured Communication-Based  
Programming Revisited:  
*Two Systems for  
Higher-Order Session Communication*

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# What do we have?

- A proof of type preservation formalised in Coq using `ssreflect`.
- A library to implement locally nameless with multiple name scopes and handle environments in a versatile way.



TACAS 2020 **accepter paper and artefact** describing our tool and mechanisation.

- We built in-team expertise (i.e. we learned some hard lessons while struggling to finish the proof).

**What did we  
mechanise?**

# A tale of three systems

- We set out to represent the three systems described in the paper:
- The Honda, Vasconcelos, Kubo system from ESOP'98
- Its naïve but ultimately unsound extension
- Its revised system inspired by Gay and Hole in Acta Informatica

# The Send Receive System

We consider terms up-to  $\alpha$ -conversion

$\text{test } a(k) \text{ in } P$   
 $\text{throw } k[k']; P$   
 $\text{catch } k(k') \text{ in } P$   
 $\text{if } e \text{ then } P \text{ else } Q$   
 $P \mid Q$   
 $\text{inact}$   
 $(\nu u)P$   
 $\text{def } D \text{ in } P$   
 $X[\tilde{e}\tilde{k}]$

$e ::= c$   
 $\mid e + e' \mid e - e' \mid e \times e \mid \text{not}(e) \mid \dots$

$D ::= X_1(\tilde{x}_1\tilde{k}_1) = P_1 \text{ and } \dots \text{ and } X_n(\tilde{x}_n\tilde{k}_n) = P_n$  declare

session request  
 session acceptance  
 data sending  
 data reception  
 label selection  
 label branching  
 name binding

Then we cannot distinguish:  
 $k?(x) \text{ in inact}$   
 and  
 $k?(y) \text{ in inact}$



# $\alpha$ -conversion curse or Blessing?

$$(\text{throw } k[\underline{k'}]; P_1) \mid (\text{catch } k(\underline{k'}) \text{ in } P_2) \rightarrow P_1 \mid P_2$$

- The original system depends crucially on names

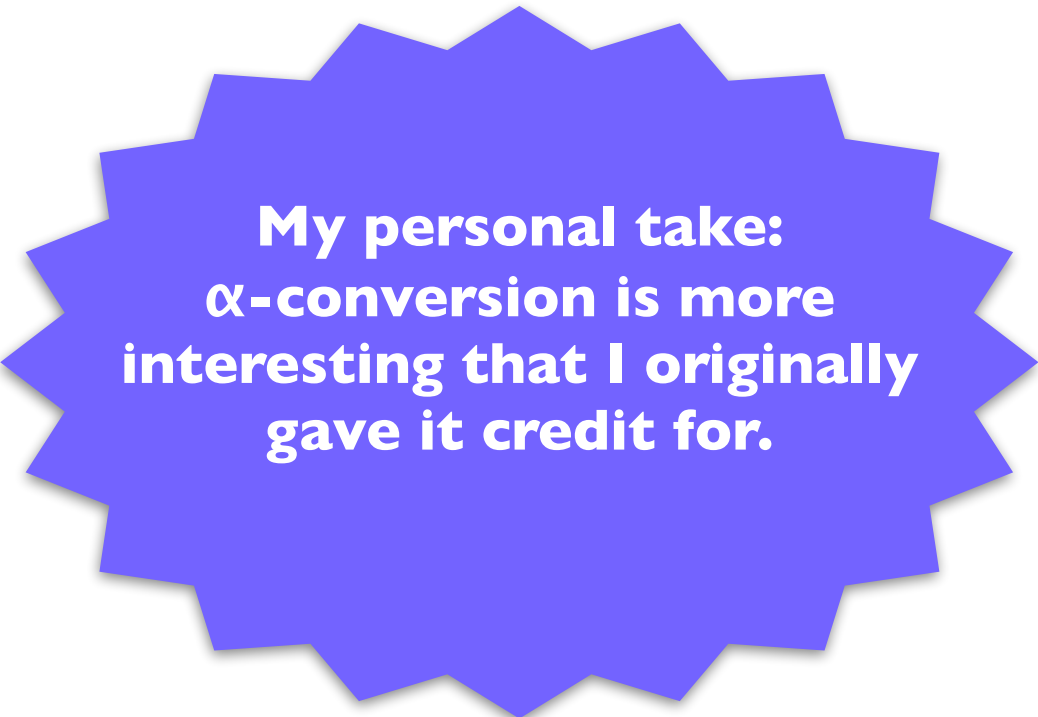
**This is a bound variable.**

- If  $\alpha$ -conversion is built in, this rule collapses to:

$$(\text{throw } k[k']; P_1) \mid (\text{catch } k(k'') \text{ in } P_2) \rightarrow P_1 \mid P_2[k'/k'']$$

# $\alpha$ -conversion curse or Blessing?

- Humans have to pretend not to see the different bound names.
- However, there exist several representations that offer inherently  $\alpha$ -convertible terms:
  - de Bruijn indices (or levels)
  - Higher Order Abstract Syntax
  - Locally Nameless



**My personal take:  
 $\alpha$ -conversion is more  
interesting that I originally  
gave it credit for.**

# The Naïve Representation

- It “**looks like**” the original Send Receive system.
- You start **suspecting** is wrong when defining the reduction relation.
- You **know** there is a problem when the proof fails.

# The Revisited system

- Now we distinguish between the endpoints of channels.
- It can be readily represented with LN-variables and names.

# Four kinds of atoms

Inductive proc : Set :=

| request : scvar → proc → proc  
| accept : scvar → proc → proc

| send : channel → exp → proc → proc  
| receive : channel → proc → proc

| select :  
  channel → label → proc → proc  
| branch :  
  channel → proc → proc → proc

| throw :  
  channel → channel → proc → proc  
| catch : channel → proc → proc

| ife : exp → proc → proc → proc  
| par : proc → proc → proc  
| inact : proc

(\* hides a channel name \*)

| nu\_ch : proc → proc

(\* hides a name \*)

| nu\_nm : proc → proc

(\* process replication \*)

| bang : proc → proc

.

binds variable  
from  $A_{SC}$

binds variable  
from  $A_{EV}$

binds variable  
from  $A_{LC}$

binds channel  
from  $A_{CN}$



# Typing environments

- Store their assumptions in a unique order  
**(easy to compare)**
- Only store unique assumptions  
**(easy to split)**
- They come with many lemmas  
**(less induction proofs)**



These are generic enough  
and easy to use. #artefact

# Subject Reduction

**Theorem 3.3 (Subject Reduction)** *If  $\Theta; \Gamma \vdash P \triangleright \Delta$  with  $\Delta$  balanced and  $P \rightarrow^* Q$ , then  $\Theta; \Gamma \vdash Q \triangleright \Delta'$  and  $\Delta'$  balanced.*

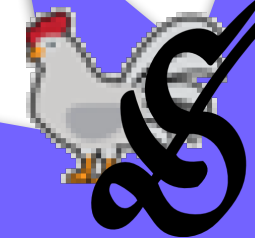
**Is straightforward to represent:**

```
Theorem SubjectReduction G P Q D:  
  oft G P D → balanced D → P →* Q → exists D', balanced D' /\ oft G Q D'.
```

**We want more from  
our mechanisation.**



# Motivating Meta-Theory



**Certified  
Scribble  
Algorithms**

**Certified tool + reasoning environment**

**About  
Processes**

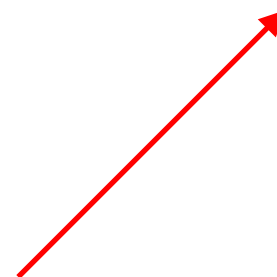
**Reasoning**

**Certified code  
extraction**

**Processes  
into OCaml**

**Mechanised  
Meta-theory**

**MPST Trace equivalence**



# Processes : Local Types



```
Inductive l_ty :=
| l_end
| l_var (v : ℕ)
| l_rec (L : l_ty)
| l_msg (a : l_act) (r : role) (Ks : seq (lbl * (mty * l_ty)))
.

--:--- Local.v          2% (21,3)    Git:master (Coq 🐔 yas hs Outl
Wrote /Users/franciscoferreira/devel/cmpst/theories/Proc.v
```

# Processes



```
Inductive Proc : l_ty → Type :=
| Finish : Proc l_end

| Var : ∀ (v : ℕ), Proc (l_var v)
| Rec L: Proc L → Proc (l_rec L)

| Recv a (p : role) : Alts a → Proc (l_msg l_recv p a)
| Send (p : role) L a T (l : lbl) :
  coq_ty T →
  Proc L →
  (l, (T, L)) \in a →
  Proc (l_msg l_send p a)

with Alts : seq (lbl * (mtty * l_ty)) → Type :=
| A_sing T L l : (coq_ty T → Proc L) → Alts [:: (l, (T, L))]
| A_cons T L a l : (coq_ty T → Proc L) →
  Alts a →
  Alts ((l, (T, L)) :: a)

.□
```

```
--:--- Proc.v 5% (47,1) Git:master (Coq Script(0-))
Wrote /Users/franciscoferreira/devel/cmpst/theories/Proc.v
```

# “Process Traces are Nice”



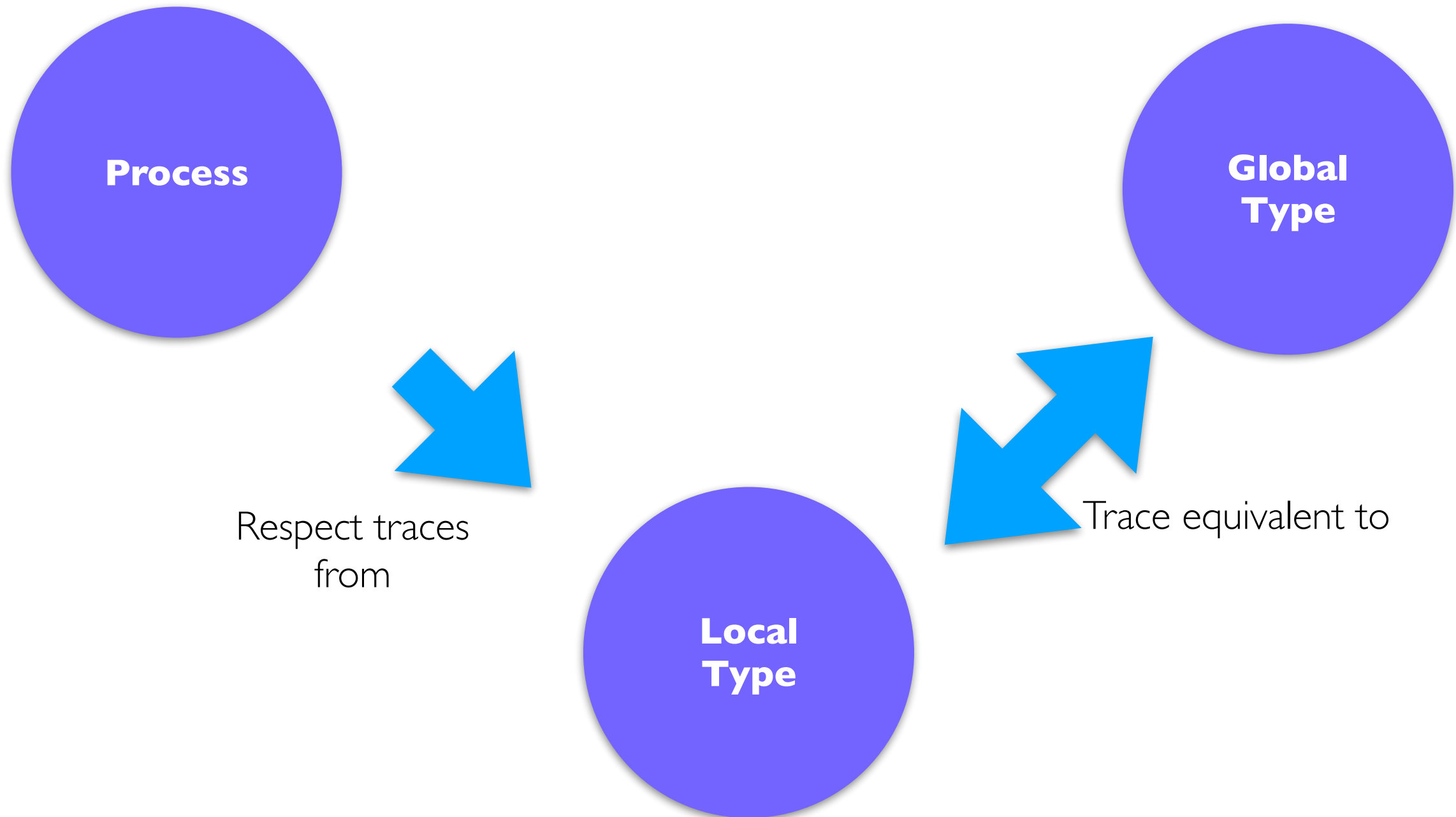
```
Proc.v

Definition run_rt_act L (P : Proc L) (A : rt_act) : (Proc (run_act_l_ty L (erase_act A))).□

-:--- Proc.v      83% (366,94)  Git:master  (Coq Script(0-) 🐔 yas hs Outl company Holes)
Wrote /Users/franciscoferreira/devel/cmpst/theories/Proc.v
```

- Running a process preserves types by construction

# From Processes to...



# Reasoning

- A process is a term of type `Proc L`.
- The user just writes proofs on the shape of said term.
- Processes are translated into monadic computations.

# Extraction of certified code

- Two aspects:
  - Generating certified OCaml code parametrised by an ambient monad.
  - Generating a certified library to handle Multiparty Session Types. Ultimately combining the  $\nu$ Scr (a small implementation of Scribble in OCaml) to build **Certified  $\nu$ Scr**.

# Certified Processes



```
Proc.v
From Coq Require Extraction.
Module MP.
  Parameter t : Type → Type.

  Parameter send : ∀ T, role → lbl → T → t unit.
  (* Extract Constant send ⇒ "ocaml_send". *)

  Parameter recv : (lbl → t unit) → t unit.
  Parameter recv_one : ∀ T, role → t T.

  Parameter bind : ∀ T1 T2, t T1 → (T1 → t T2) → t T2.

  Parameter pure : ∀ T1, T1 → t T1.

  Parameter loop : ∀ T1, ℕ → t T1 → t T1.
  Parameter set_current : ℕ → t unit.
End MP.

-:--- Proc.v 14% (67,0) Git:master (Coq Script(0.
```



# About Proof Assistant Choice

- We chose Coq because it is powerful, well maintained, and popular in PL.
- While using it,
  - 😞 I wished for Isabelle's automation and classical logic.
  - 😭 I cried over the loss of Agda's dependent pattern matching and rich interaction with the system.
  - 😓 As we try to get extraction to work, I envy Idris's compiler.

# If you want to know more...

- Talk to us!
- Binary Session types:
  - TACAS'20 Tool Paper: <https://bit.ly/3co7KFn>
  - Tech report: <https://bit.ly/2ZZzAVE>
  - EMTST repository: <https://github.com/emtst/>
- Multiparty Session Types
  - Repo: [Talk to us!](#)
  - Check vScr at: <https://nuscr.github.io>



**Thanks for your  
kind attention!  
Questions?**